basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

SENIOR CERTIFICATE EXAMINATIONS/
NATIONAL SENIOR CERTIFICATE EXAMINATIONS

MATHEMATICS P2/*WISKUNDE V2*

MAY/JUNE 2025/*MEI/JUNIE 2025*

MARKING GUIDELINES/*NASIENRIGLYNE*

MARKS/*PUNTE*: 150

These marking guidelines consist of 23 pages.
Hierdie nasienriglyne bestaan uit 23 bladsye.

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NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

LET WEL:

- *As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.*
- *As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.*
- *Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.*
- *Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat NIE.*

GEOMETRY • MEETKUNDE	
S	**A mark for a correct statement** **(A statement mark is independent of a reason)**
	'n Punt vir 'n korrekte bewering **('n Punt vir 'n bewering is onafhanklik van die rede)**
R	**A mark for the correct reason** **(A reason mark may only be awarded if the statement is correct)**
	'n Punt vir 'n korrekte rede **('n Punt word slegs vir die rede toegeken as die bewering korrek is)**
S/R	**Award a mark if statement AND reason are both correct**
	Ken 'n punt toe as die bewering EN rede beide korrek is

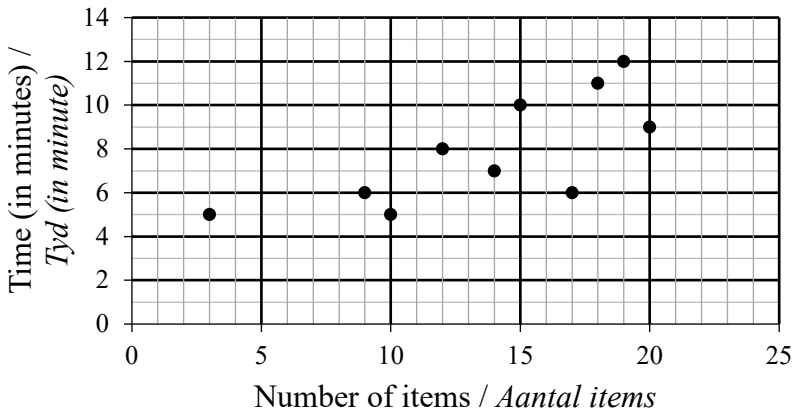
QUESTION/*VRAAG* 1

134	215	325	326	362	429	515	531	598	610	624	728	923	1 034	1 200

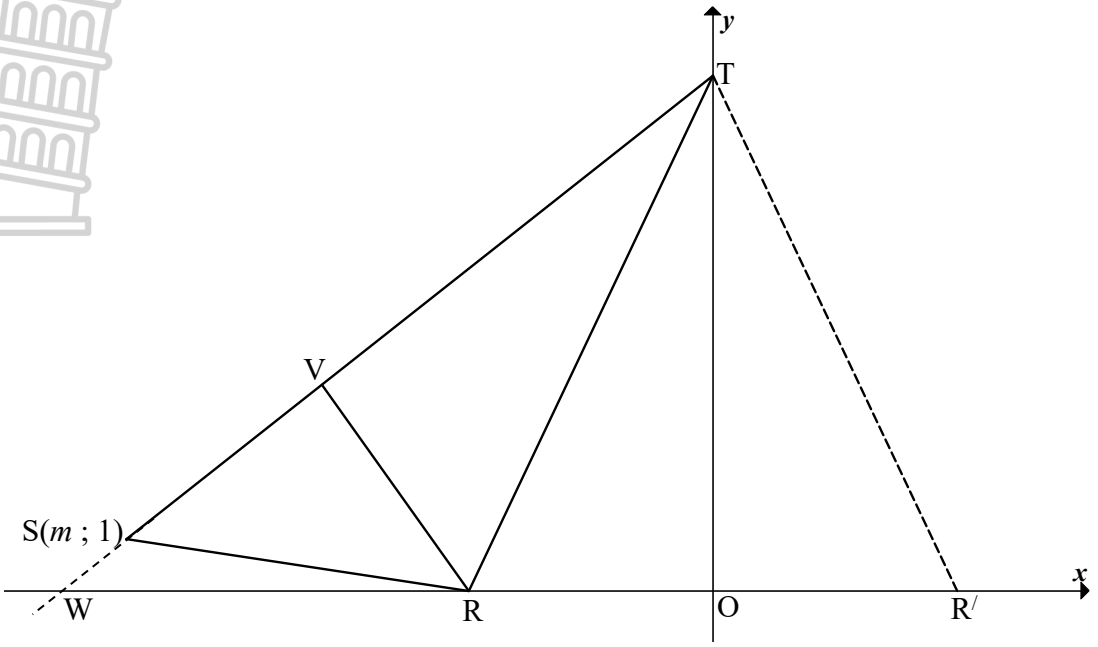
1.1	$\bar{x} = \frac{8554}{15}$ $= 570{,}27$	✓ 8554 ✓ answer (2)
1.2	$\sigma = 291{,}03$	✓ 291,03 (1)
1.3	$(279{,}24\ ;\ 861{,}3)$ $\therefore 10$ premiums	✓ $(\bar{x} - \sigma\ ;\ \bar{x} + \sigma)$ ✓ answer (2)
1.4	$\frac{\left(1791 \times \frac{118}{100}\right) + \left(6763 \times \frac{k+100}{100}\right)}{15} = 686{,}44$ $6763 \times \frac{k+100}{100} = 8183{,}22$ $\frac{k+100}{100} = 1{,}209...$ $k + 100 = 120{,}999...$ $k = 21\%$	✓ $1791 \times \frac{118}{100}$ ✓ $6763 \times \frac{k+100}{100}$ ✓ $\frac{\text{sum of new premiums}}{15} = 686{,}44$ ✓ answer (4)
		[9]

QUESTION/*VRAAG* 2

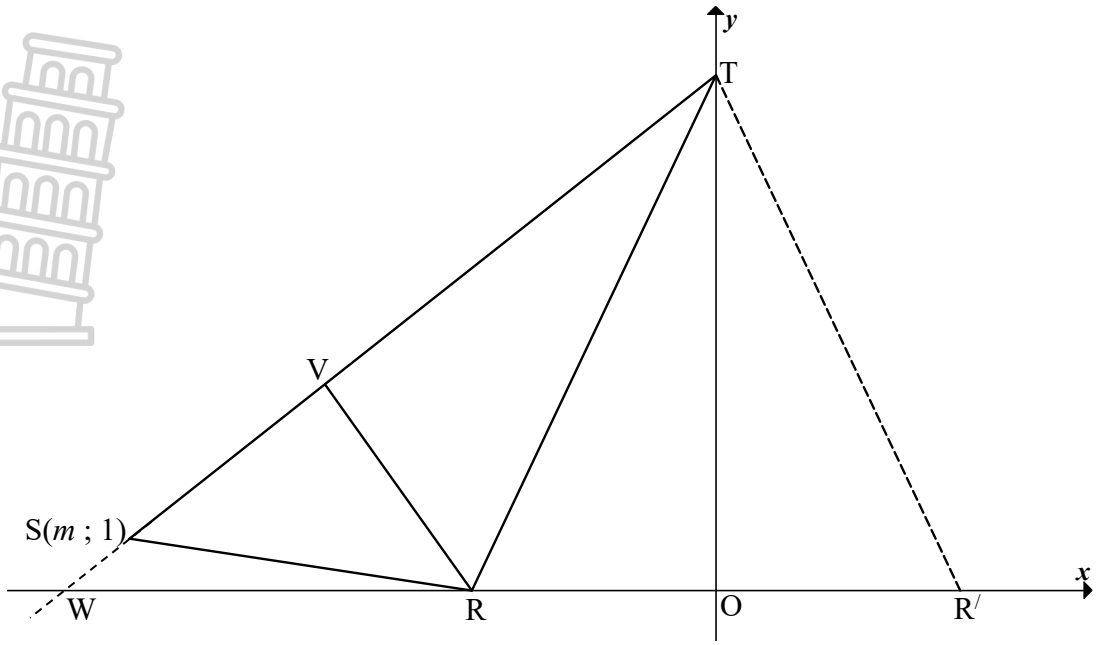
Number of items/*Aantal items* (*x*)	10	3	20	14	17	9	12	18	15	19
Time (in minutes)/*Tyd in minute)* (*y*)	5	5	9	7	6	6	8	11	10	12

2.1	**Scatter plot / *Spreidiagram***  	✓ 3 points correct ✓ 6 points correct ✓ all points correct (3)
2.2	$a = 3{,}079\ldots$ $b = 0{,}351\ldots$ $\hat{y} = 3{,}08 + 0{,}35x$	✓ $a = 3{,}08$ ✓ $b = 0{,}35$ ✓ equation (3)
2.3	$r = 0{,}74$	✓ 0,74 (1)
2.4	$y = 3{,}08 + 0{,}35(13)$ $y = 7{,}63$ **OR** $y = 7{,}65$ (calculator)	✓ substitute x=13 ✓ answer (2) ✓✓ 7,65 (2)
2.5	It does not make sense to **pack 0** items in **3,08 minutes./** *Dit maak nie sin dat **0 items** in **3,08 minute** gepak kan word nie.*	✓ answer (1)
		[10]

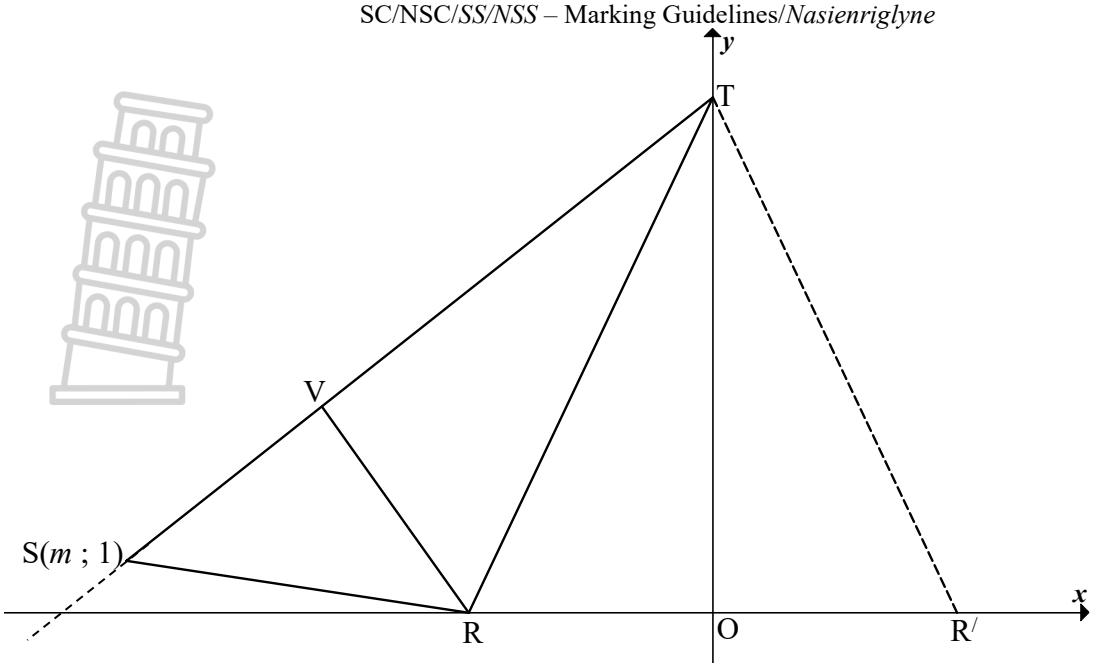
QUESTION/*VRAAG* 3



3.1	$2x - y + 10 = 0$ $2x - 0 + 10 = 0$ $x = -5$ R(–5 ; 0)	✓ $y = 0$ ✓ $x = -5$ (2)
3.2	R(–5 ; 0) T(0 ; 10) $(RT)^2 = (-5-0)^2 + (0-10)^2$ **OR** $(RT)^2 = 5^2 + 10^2$ (Pythag) $RT = \sqrt{125}$ units **OR/*OF*** $RT = 5\sqrt{5}$ units	✓ T(0 ; 10) ✓ subst of R & T into distance formula or Pythagoras ✓ answer (3)
3.3	$2RT^2 = 5SR^2$ $2(125) = 5[(m-(-5))^2 + (1-0)^2]$ $5[(m+5)^2 + (1)^2] = 250$ $(m+5)^2 + 1 = 50$ $m^2 + 10m - 24 = 0$ **OR/*OF*** $(m+5)^2 = 49$ $(m-2)(m+12) = 0$ $m+5 = \pm 7$ $m = -5 \pm 7$ $m = 2$ or $m = -12$ $m = 2$ or $m = -12$ N/A N/A $\therefore m = -12$ $\therefore m = -12$	✓ length of $2RT^2$ ✓ length of $5SR^2$ ✓ standard form or isolating square ✓ negative answer (4)

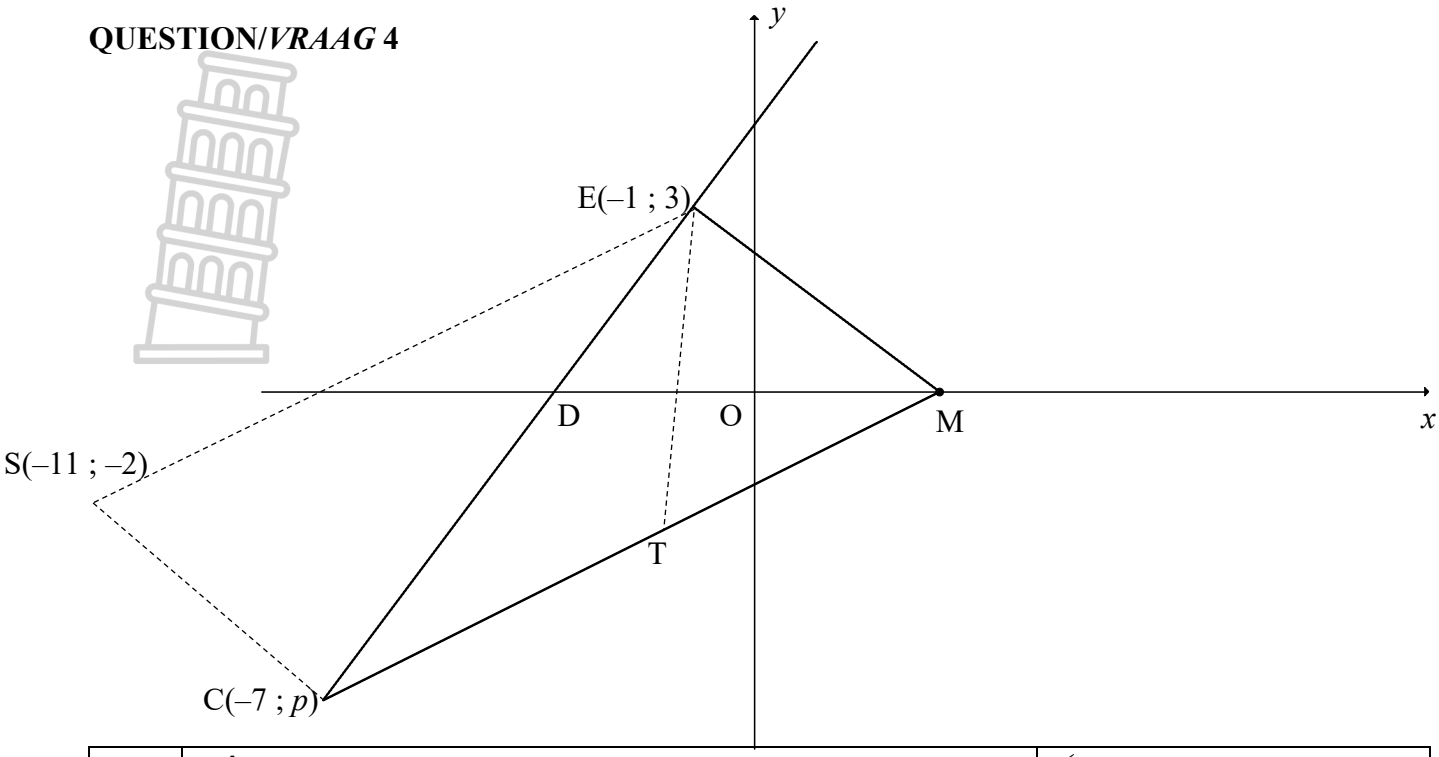


3.4	$m_{ST} = \frac{1-10}{-12-0}$ $m_{ST} = \frac{3}{4}$ $\therefore m_{VR} = -\frac{4}{3}$ $y = -\frac{4}{3}x + c$ $0 = -\frac{4}{3}(-5) + c$ $c = -\frac{20}{3}$ $y = -\frac{4}{3}x - \frac{20}{3}$	**OR/*OF*** $y - y_1 = -\frac{4}{3}(x - x_1)$ $y - 0 = -\frac{4}{3}(x - (-5))$ $y = -\frac{4}{3}(x + 5)$ $y = -\frac{4}{3}x - \frac{20}{3}$	✓ substitution of S & T into gradient formula ✓ m_{ST} ✓ $m_{VR} = -\frac{1}{m_{ST}}$ ✓ substitution of R ✓ equation (5)
3.5	VR: $y = -\frac{4}{3}x - \frac{20}{3}$ ST: $y = \frac{3}{4}x + 10$ $\frac{3}{4}x + 10 = -\frac{4}{3}x - \frac{20}{3}$ $9x + 120 = -16x - 80$ $25x = -200$ $x = -8$ $y = 4$ $\therefore V(-8 ; 4)$		✓ equating VR and ST ✓ simplification leading to $x = -8$ (2)



3.6	$R'(5;0)$	
	$VR = \sqrt{[-8-(-5)]^2+(4-0)^2} = 5$	✓ length of VR
	$VT = \sqrt{(-8-0)^2+(4-10)^2} = 10$	✓ length of VT
	Area of $RVTR' = \frac{1}{2}(VR)(VT)+\frac{1}{2}(RR')(OT)$	
	$= \frac{1}{2}(5)(10)+\frac{1}{2}(10)(10)$	✓ area ΔVRT ✓ area Δ RTR′
	$= 25 + 50$	
	$= 75\text{ units}^2$	✓ answer
	OR/*OF*	(5)
	ST: $y = \frac{3}{4}x + 10$	
	$0 = \frac{3}{4}x + 10$	
	$x = -\frac{40}{3}$ or $-13\frac{1}{3}$	✓ *x*-intercept of ST
	$W\left(-\frac{40}{3};0\right)$	
	$WR' = 5-\left(-\frac{40}{3}\right) = \frac{55}{3} = 18\frac{1}{3}$	✓ length of WR′
	Area of $RVTR'$ = Area of $\Delta TWR'$ − Area of ΔWVR	
	$= \frac{1}{2}\left(5+\frac{40}{3}\right)(10)-\frac{1}{2}\left(-5+\frac{40}{3}\right)(4)$	✓ area Δ TWR′ ✓ area Δ WVR
	$= 75\text{ units}^2$	✓ answer
		(5)
		[21]

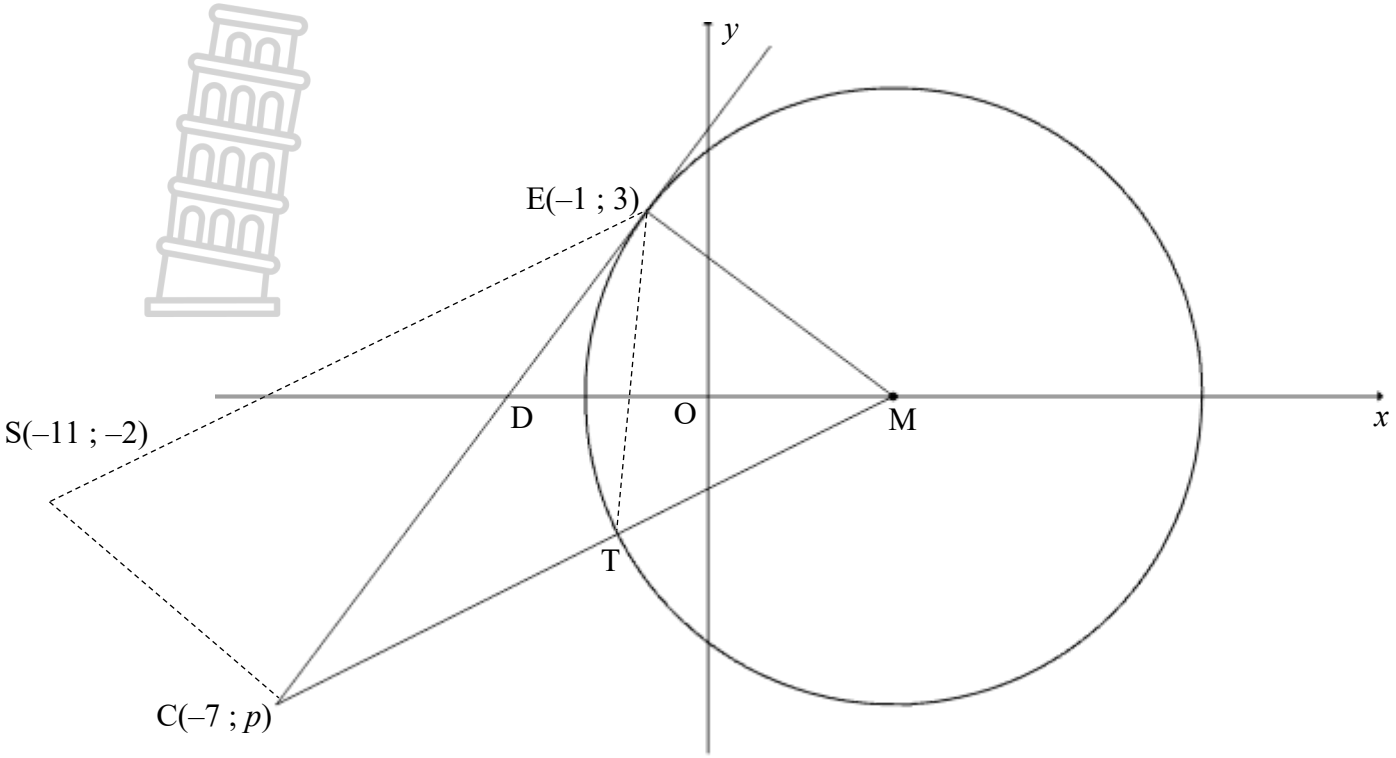
QUESTION/*VRAAG* 4



4.1	$C\hat{E}M = 90°$	✓ answer (1)
4.2	$m_{ME} = \frac{0-3}{3-(-1)}$ $m_{ME} = -\frac{3}{4}$ $\therefore m_{ED} = \frac{4}{3}$ $3 = \frac{4}{3}(-1) + c$ **OR/*OF*** $y - 3 = \frac{4}{3}(x-(-1))$ $y = \frac{4}{3}x + \frac{13}{3}$ $y = \frac{4}{3}x + \frac{13}{3}$ **OR/*OF*** $DM = \sqrt{(5)^2 + \left(\frac{15}{4}\right)^2}$ [Pythagoras] $DM = \frac{25}{4}$ or 6,25 units $\therefore D\left(-\frac{13}{4};0\right)$ $m_{ED} = \frac{3-0}{-1-\left(-\frac{13}{4}\right)}$ $\therefore m_{ED} = \frac{4}{3}$ $3 = \frac{4}{3}(-1) + c$ **OR/*OF*** $y - 3 = \frac{4}{3}(x-(-1))$ $y = \frac{4}{3}x + \frac{13}{3}$ $y = \frac{4}{3}x + \frac{13}{3}$	✓ $m_{ME} = -\frac{3}{4}$ ✓ m_{ED} ✓ substitution of E(–1 ; 3) ✓ equation (4) ✓ coordinates of D ✓ m_{ED} ✓ substitution of E(–1 ; 3) ✓ equation (4)

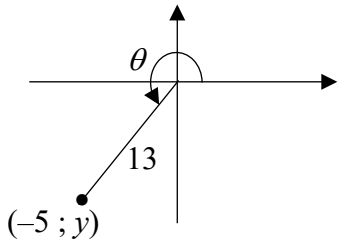
4.3	$y=\frac{4}{3}x+\frac{13}{3}$ $0=\frac{4}{3}x+\frac{13}{3}$ $x_D=-\frac{13}{4}$	✓ x_D
	$\therefore DM=3-\left(-\frac{13}{4}\right)$	✓ x_M-x_D
	$DM=\frac{25}{4}$ or $6{,}25$ units	✓ answer (3)
	OR/*OF*	
	EM = 5 units $ED=\frac{15}{4}$ units	✓ EM = 5 units
	$DM=\sqrt{(5)^2+\left(\frac{15}{4}\right)^2}$ [Pythagoras] $DM=\frac{25}{4}$ or $6{,}25$ units	✓ substitution of EM & ED ✓ answer (3)
4.4	EC: $y=\frac{4}{3}x+\frac{13}{3}$ $p=\frac{4}{3}(-7)+\frac{13}{3}$ $p=-5$	✓ substitution of C(–7 ; *p*) into equation of EC (1)
	OR/*OF*	
	$m_{EC}=\frac{4}{3}$ $\frac{p-3}{-7-(-1)}=\frac{4}{3}$ $p-3=\frac{4}{3}(-6)$ $p=-5$	✓ substitution of C(–7 ; *p*) into gradient of EC (1)

4.5	$M \rightarrow E: (x\ ;\ y) \rightarrow (x - 4\ ;\ y + 3)$ [translation] $C \rightarrow S: (-7\ ;\ -5) \rightarrow (-7 - 4\ ;\ -5 + 3)$ $\therefore S(-11\ ;\ -2)$ **OR/*OF*** $M \rightarrow C: (x\ ;\ y) \rightarrow (x - 10\ ;\ y - 5)$ [translation] $E \rightarrow S: (-1\ ;\ 3) \rightarrow (-1 - 10\ ;\ 3 - 5)$ $\therefore S(-11\ ;\ -2)$ **OR/*OF*** E(–1 ; 3) and C(–7 ; –5) $\left(\frac{-1+(-7)}{2}\ ;\ \frac{3+(-5)}{2}\right)$ [Midpoint of EC] $=(-4;-1)$ S(x ; y) and M(3 ; 0) $\frac{x_S+3}{2}=-4 \qquad \frac{y_S+0}{2}=-1$ $x_S=-11 \qquad y_S=-2$ $\therefore S(-11\ ;\ -2)$	✓ method: translation ✓ $x_S=-11$ ✓ $y_S=-2$ (3) ✓ method: translation ✓ $x_S=-11$ ✓ $y_S=-2$ (3) ✓ method: midpoint ✓ $x_S=-11$ ✓ $y_S=-2$ (3)
4.6	$r_{NEW}=5+7$ $r_{NEW}=12$ $MS=\sqrt{(3-(-11))^2+(0-(-2))^2}$ MS = $\sqrt{200}$ or $10\sqrt{2}$ or 14,14 units 14,14 > 12 $\therefore S(-11;-2)$ lies outside the circle	✓ $r_{NEW}=12$ ✓ MS ✓ conclusion (3)



4.7	Inclination of EM: $\tan \hat{M} = m_{ME} = -\frac{3}{4}$ ref. $\angle = 36{,}87°$ Inclination of EM = 143,13° $\therefore E\hat{M}D = 36{,}87°$ Inclination of CM: $\tan \hat{M} = m_{CM} = \frac{5}{10}$ or $\frac{1}{2}$ $\therefore \hat{M} = 26{,}57°$ $\therefore E\hat{M}T = 26{,}57° + 36{,}87°$ $= 63{,}44°$ But EM = MT [radii] $\therefore E\hat{T}M = \frac{180° - 63{,}44°}{2}$ $\therefore E\hat{T}M = 58{,}28°$	✓ inclination of EM ✓ $E\hat{M}D$ ✓ inclination of CM ✓ $E\hat{M}T$ ✓ answer (5)
		[20]

QUESTION/*VRAAG* 5

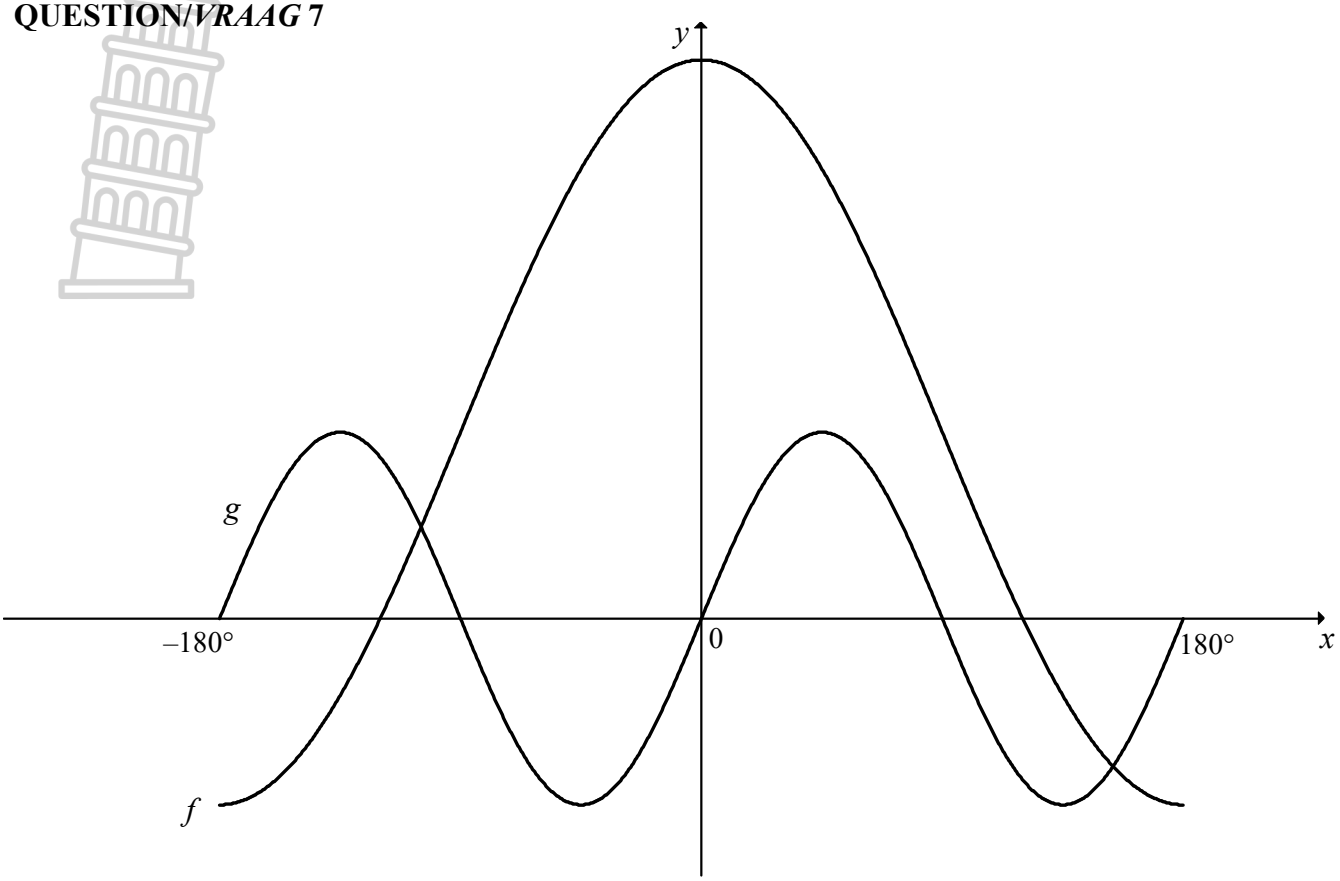
5.1.1	$y^2 = \sqrt{13^2 - (-5)^2}$ [Pythagoras] $y = -12$ $\sin^2\theta$ $= \left(-\frac{12}{13}\right)^2$ $= \frac{144}{169}$ **OR/*OF*** $\sin^2\theta = 1 - \cos^2\theta$ $\sin^2\theta = 1 - \left(-\frac{5}{13}\right)^2$ $\sin^2\theta = \frac{144}{169}$ 	✓ $y = -12$ ✓ substitution ✓ answer (3) ✓ square identity ✓ substitution ✓ answer (3)
5.1.2	$\tan(360° - \theta)$ $= -\tan\theta$ $= -\left(\frac{-12}{-5}\right)$ $= -\frac{12}{5}$	✓ $-\tan\theta$ ✓ answer (2)
5.1.3	$\cos(\theta - 135°)$ $= \cos\theta\cos 135° + \sin\theta\sin 135°$ $= \cos\theta(-\cos 45°) + \sin\theta(\sin 45°)$ $= \left(-\frac{5}{13}\right)\left(-\frac{\sqrt{2}}{2}\right) + \left(-\frac{12}{13}\right)\left(\frac{\sqrt{2}}{2}\right)$ OR $\left(-\frac{5}{13}\right)\left(-\frac{1}{\sqrt{2}}\right) + \left(-\frac{12}{13}\right)\left(\frac{1}{\sqrt{2}}\right)$ $= -\frac{7\sqrt{2}}{26}$ $= -\frac{7}{13\sqrt{2}}$	✓ cpd. ∠ expansion ✓ reduction ✓ substitution ✓ answer (4)

5.2	$\frac{2\cos(180°-x)\sin(-x)}{1-2\cos^2(90°-x)}$ $=\frac{2(-\cos x)(-\sin x)}{1-2\sin^2 x}$ $=\frac{2\sin x\cos x}{\cos 2x}$ $=\frac{\sin 2x}{\cos 2x}$ $=\tan 2x$	✓ $\cos(180°-x)=-\cos x$ ✓ $\sin(-x)=-\sin x$ ✓ $\cos^2(90°-x)=\sin^2 x$ ✓ $1-2\sin^2 x=\cos 2x$ ✓ $2\sin x\cos x=\sin 2x$ ✓ answer (6)
5.3	$(\tan 92°)(\tan 94°)(\tan 96°)...(\tan 176°)(\tan 178°)$ $=\left(\frac{\sin 92°}{\cos 92°}\right)\left(\frac{\sin 94°}{\cos 94°}\right)\left(\frac{\sin 96°}{\cos 96°}\right)...\left(\frac{\sin 176°}{\cos 176°}\right)\left(\frac{\sin 178°}{\cos 178°}\right)$ $=\left(\frac{\cos 2°}{-\sin 2°}\right)\left(\frac{\cos 4°}{-\sin 4°}\right)\left(\frac{\cos 6°}{-\sin 6°}\right)...\left(\frac{\sin 4°}{-\cos 4°}\right)\left(\frac{\sin 2°}{-\cos 2°}\right)$ $=1$ **OR** $(\tan 92°)(\tan 94°)(\tan 96°)...(\tan 176°)(\tan 178°)$ $=(\tan 92°)(\tan 94°)(\tan 96°)....(-\tan 4°)(-\tan 2°)$ $=\left(\frac{\sin 92°}{\cos 92°}\right)\left(\frac{\sin 94°}{\cos 94°}\right)\left(\frac{\sin 96°}{\cos 96°}\right)...\left(-\frac{\sin 4°}{\cos 4°}\right)\left(-\frac{\sin 2°}{\cos 2°}\right)$ $=\left(\frac{\cos 2°}{-\sin 2°}\right)\left(\frac{\cos 4°}{-\sin 4°}\right)\left(\frac{\cos 6°}{-\sin 6°}\right)...\left(-\frac{\sin 4°}{\cos 4°}\right)\left(-\frac{\sin 2°}{\cos 2°}\right)$ $=1$	✓ quotient identity ✓ co-ratios ✓ reduction ✓ answer (4) ✓ reduction ✓ quotient identity ✓ co-ratios ✓ answer (4)
		[19]

QUESTION/*VRAAG* 6

6.1	$\text{LHS} = 2\cos^2(45° + x)$ $= 2\cos^2(45° + x) + 1 - 1$ $= \cos\left[2(45° + x)\right] + 1$ $= \cos(90° + 2x) + 1$ $= (-\sin 2x) + 1$ $= 1 - \sin 2x$ $= \text{RHS}$ **OR/*OF*** $\text{LHS} = 2\cos^2(45° + x)$ $= 2\left(\cos(45° + x)\right)^2$ $= 2(\cos 45° \cos x - \sin 45° \sin x)^2$ $= 2\left(\frac{\sqrt{2}}{2}\cos x - \frac{\sqrt{2}}{2}\sin x\right)^2$ $= 2\left(\frac{1}{2}\cos^2 x - \sin x \cos x + \frac{1}{2}\sin^2 x\right)$ $= \cos^2 x - 2\sin x \cos x + \sin^2 x$ $= 1 - \sin 2x$ $= \text{RHS}$	✓ + 1 – 1 ✓ double angle ✓ simplification ✓ reduction (4) ✓ compound ∠ expansion ✓ subst. special ∠ values ✓ simplification ✓ $\sin^2 x + \cos^2 x = 1$ (4)
6.2.1	$\text{LHS} = \sin(A - B) - \sin(A + B)$ $= \sin A \cos B - \cos A \sin B - (\sin A \cos B + \cos A \sin B)$ $= \sin A \cos B - \cos A \sin B - \sin A \cos B - \cos A \sin B$ $= -2\cos A \sin B$ $= \text{RHS}$	✓ $\sin A \cos B - \cos A \sin B$ ✓ $-\sin A \cos B - \cos A \sin B$ (2)
6.2.2	$\sin 4x - \sin 10x$ $= \sin(7x - 3x) - \sin(7x + 3x)$ $= -2\cos 7x \sin 3x$	✓ $4x = 7x - 3x$ & $10x = 7x + 3x$ ✓ answer (2)
6.2.3	$\sin 4x - \sin 10x = \sin 3x$ $-2\cos 7x \sin 3x = \sin 3x$ $2\cos 7x \sin 3x + \sin 3x = 0$ $\sin 3x(2\cos 7x + 1) = 0$ $\sin 3x = 0$ or $\cos 7x = -\frac{1}{2}$ $3x = 0°$ $7x = 120°$ or $7x = 240°$ $x = 0°$ $x = 17{,}14°$ $x = 34{,}29°$ N/A	✓ substitution ✓ factorisation ✓ both equations ✓ answer ✓ answer (5)
		[13]

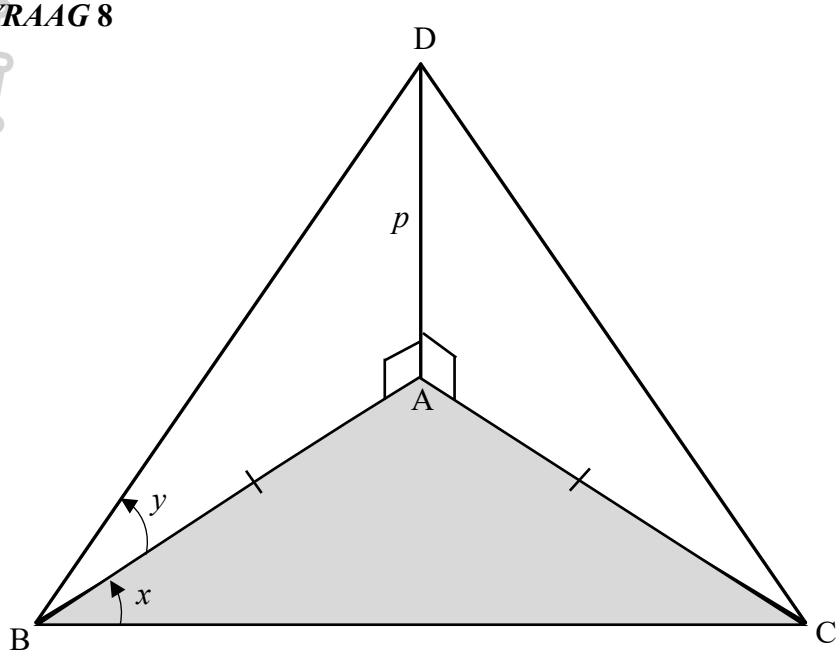
QUESTION/*VRAAG* 7



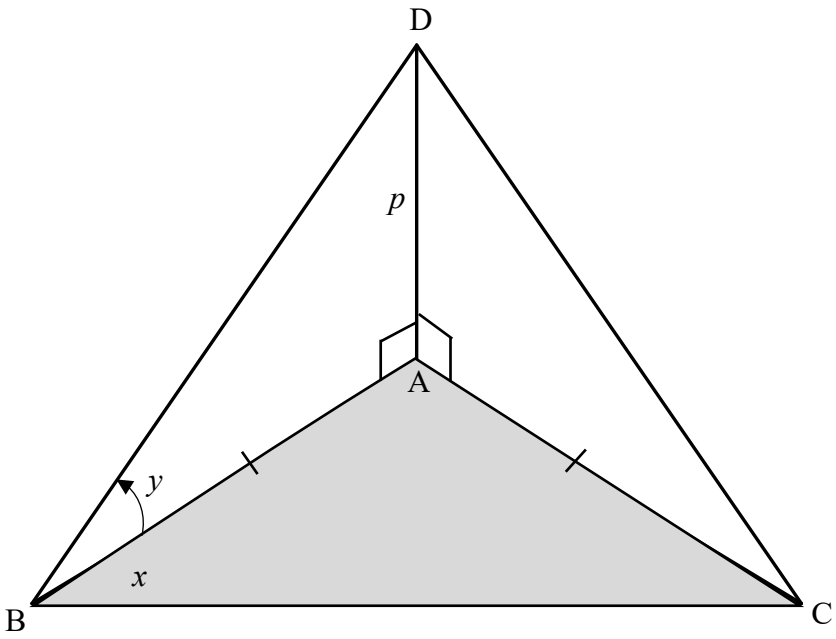
7.1	Range of f: $y \in [-1\,;\,3]$ **OR/*OF*** $-1 \le y \le 3$	✓ $y \in [-1\,;\,3]$ (1) ✓ $-1 \le y \le 3$ (1)
7.2	Period of g: $180°$	✓ $180°$ (1)
7.3	f increasing: $x \in (-180°\,;\,0°)$ **OR/*OF*** $-180° < x < 0°$	✓ $x \in (-180°\,;\,0°)$ (1) ✓ $-180° < x < 0°$ (1)
7.4.1	$g(x).f'(x) < 0$ $x \in (-90°\,;\,0°) \cup (0°\,;\,90°)$ **OR/*OF*** $-90° < x < 0°$ or $0° < x < 90°$	✓ $x \in (-90°\,;\,0°)$ ✓ $x \in (0°\,;\,90°)$ (2) ✓ $-90° < x < 0°$ ✓ $0° < x < 90°$ (2)

7.4.2	$\cos x \le -\frac{1}{2}$ $2\cos x + 1 \le 0$ $x \in [-180° ; -120°] \cup [120° ; 180°]$ **OR/*OF*** $2\cos x + 1 \le 0$ $-180° \le x \le -120°$ or $120° \le x \le 180°$	✓ $2\cos x + 1 \le 0$ ✓ $x \in [-180° ; -120°]$ ✓ $x \in [120° ; 180°]$ (3) ✓ $2\cos x + 1 \le 0$ ✓ $-180° \le x \le -120°$ ✓ $120° \le x \le 180°$ (3)
7.5	$g(x) = \sin 2x$ $h(x) = \sin 2(x - 45°)$ $= \sin(2x - 90°)$ $= -\sin(90° - 2x)$ $= -\cos 2x$	✓ $\sin(2x - 90°)$ ✓ equation of h (2)
		[10]

QUESTION/*VRAAG* 8



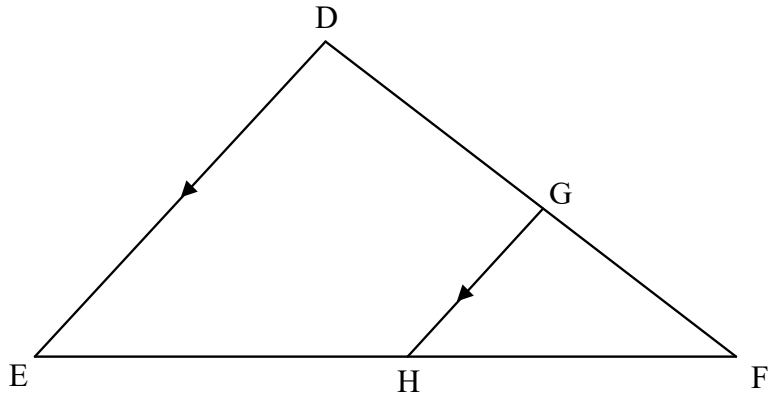
8.1	$\tan y = \frac{p}{AB}$ $AB = \frac{p}{\tan y}$	✓ correct trig ratio ✓ answer (2)
8.2	In ΔBAC: $\frac{\sin B\hat{A}C}{BC} = \frac{\sin A\hat{C}B}{AB}$ $\frac{\sin(180° - 2x)}{2p} = \frac{\sin x}{\left(\frac{p}{\tan y}\right)}$ $\frac{\sin 2x}{2p} = \sin x \times \left(\frac{\tan y}{p}\right)$ $\frac{2\sin x\cos x}{2p} = \sin x \times \left(\frac{\tan y}{p}\right)$ $2\cos x = \left(\frac{\tan y}{p}\right)(2p)$ $\cos x = \tan y$	✓ correct use of sine-rule ✓ substitute BC & AB ✓ $\sin(180° - 2x) = \sin 2x$ ✓ $\sin 2x = 2\sin x\cos x$ (4)



8.2	**OR/*OF*** In ΔBAC: $BC^2 = AB^2 + AC^2 - 2(AB)(AC)\cos B\hat{A}C$ $(2p)^2 = \left(\frac{p}{\tan y}\right)^2 + \left(\frac{p}{\tan y}\right)^2 - 2\left(\frac{p}{\tan y}\right)\left(\frac{p}{\tan y}\right)\cos(180° - 2x)$ $4p^2 = \frac{2p^2}{\tan^2 y} - \frac{2p^2(-\cos 2x)}{\tan^2 y}$ $4p^2\tan^2 y = 2p^2(1 + \cos 2x)$ $\tan^2 y = \frac{1 + 2\cos^2 x - 1}{2}$ $\tan^2 y = \cos^2 x$ $\tan y = \cos x$	✓ correct use of cos-rule ✓ substitute AB & BC ✓ $\cos(180° - 2x) = -\cos 2x$ ✓ $\cos 2x = 2\cos^2 x - 1$ (4)
8.3	$\cos x = \tan y$ $\tan y = \cos 60°$ $\tan y = 0,5$ $y = 26,57°$	✓ substitution of 60° ✓ answer (2)
		[8]

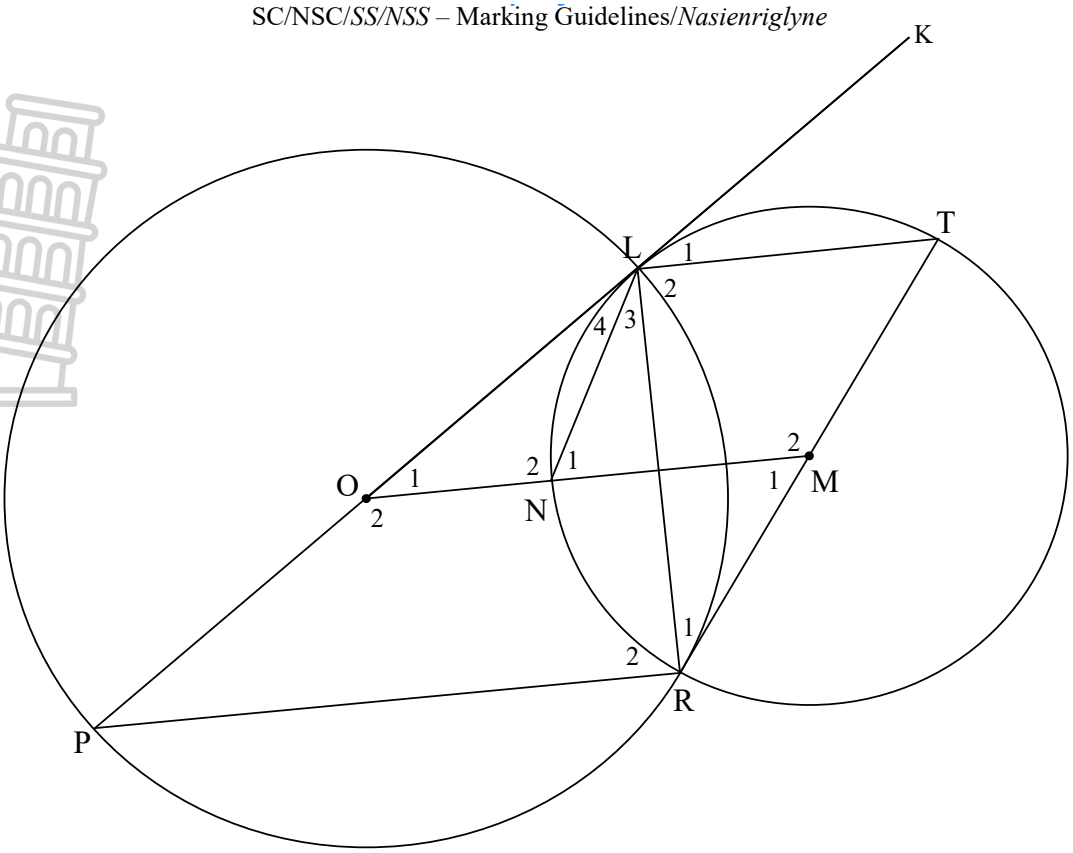
QUESTION/*VRAAG* 9

9.1



9.1.1	$\frac{HF}{EH}=\frac{GF}{GD}=\frac{2}{5}$ [line ‖ to one side of Δ/*lyn* ‖ *een sy van* Δ] **OR** [prop theorem; GH‖DE/*eweredigheidst.; GH ‖ DE*]	✓ S ✓ R (2)
9.1.2	$\frac{EH}{EF}=\frac{DG}{DF}=\frac{5}{7}$ [line ‖ to one side of Δ/*lyn* ‖ *een sy van* Δ] **OR** [prop theorem; GH‖DE/*eweredigheidst.; GH ‖ DE*] $\frac{EH}{21}=\frac{5}{7}$ $EH = 15\text{cm}$ **OR/*OF*** $\frac{HF}{EF}=\frac{2}{7}$ [line ‖ to one side of Δ/*lyn* ‖ *een sy van* Δ] **OR** [prop theorem; GH‖DE/*eweredigheidst.; GH ‖ DE*] $\frac{HF}{21}=\frac{2}{7}$ $HF = 6\text{cm}$ $EH = 21-6$ $EH = 15\text{cm}$	✓ S ✓ answer (2) ✓ S ✓ answer (2)
9.1.3	ΔFGH ||| **ΔFDE** [∠∠∠]	✓ S (1)
9.1.4	$\frac{GH}{DE}=\frac{FH}{FE}$ [|||Δ's] **OR/*OF*** $\frac{GH}{DE}=\frac{FG}{FD}$ [|||Δ's] $\frac{GH}{DE}=\frac{2}{7}$	✓ S ✓ S (2)

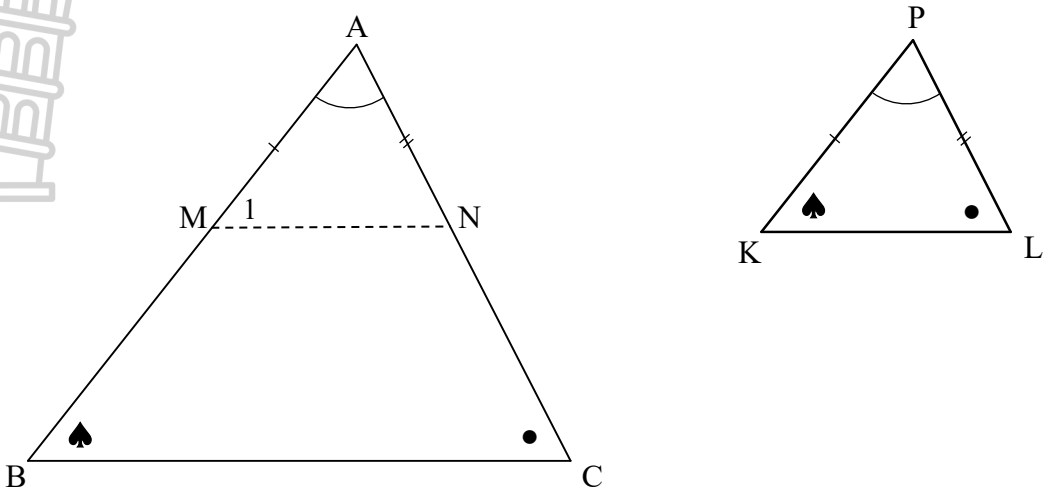
9.2



9.2.1	$\hat{L}_2 = 90°$ [∠ in semi-circle/ *∠ in halwe sirkel*] **OR** $\hat{L}_1 = \hat{R}_1$ [tan chord theorem/ *raaklyn-koordst.*] $\hat{R}_2 = 90°$ [∠ in semi-circle] *∠ in halwe sirkel*] $\hat{L}_1 = \hat{P}$ [tan chord theorem] *raaklyn-koordst.*] $\therefore \hat{L}_2 = \hat{R}_2$ $\therefore \hat{L}_1 = \hat{P}$ $\therefore$ LT ‖ PR [alt ∠s =/*verw. ∠e* =] $\therefore$ LT ‖ PR [corresp. ∠s =/ *ooreenk. ∠e* =]	✓ S ✓ R ✓ S/R ✓ R (4)
9.2.2	$\hat{L}_1 = \hat{R}_1$ [tan chord theorem/*raaklyn-koordst.*] $\hat{L}_1 = \hat{O}_1$ [corresp. ∠s; LT ‖ OM/*ooreenk. ∠e; LT ‖OM*] $\therefore \hat{R}_1 = \hat{O}_1$ $\therefore$ L, O, R and M are concyclic. $\therefore$ LORM is a cyclic quadrilateral [converse ∠s in the same seg/ *omgekeerde ∠e in dies. sirkel segm*]	✓ S ✓ R ✓ S/R ✓ S ✓ R (5)
9.2.3	$O\hat{L}R = \hat{M}_1$ [∠s in the same seg/*∠e in dieselfde segment*] $2\hat{L}_3 = \hat{M}_1$ [∠ at centre = 2 ×∠ at circumference/ *midpt. ∠ = 2× omtreks ∠*] $\therefore O\hat{L}R = 2\hat{L}_3$ $\therefore \hat{L}_4 = \hat{L}_3$ $\therefore$ LN bisects $O\hat{L}R$	✓ S/R ✓ S ✓ R ✓ S (4)
		[20]

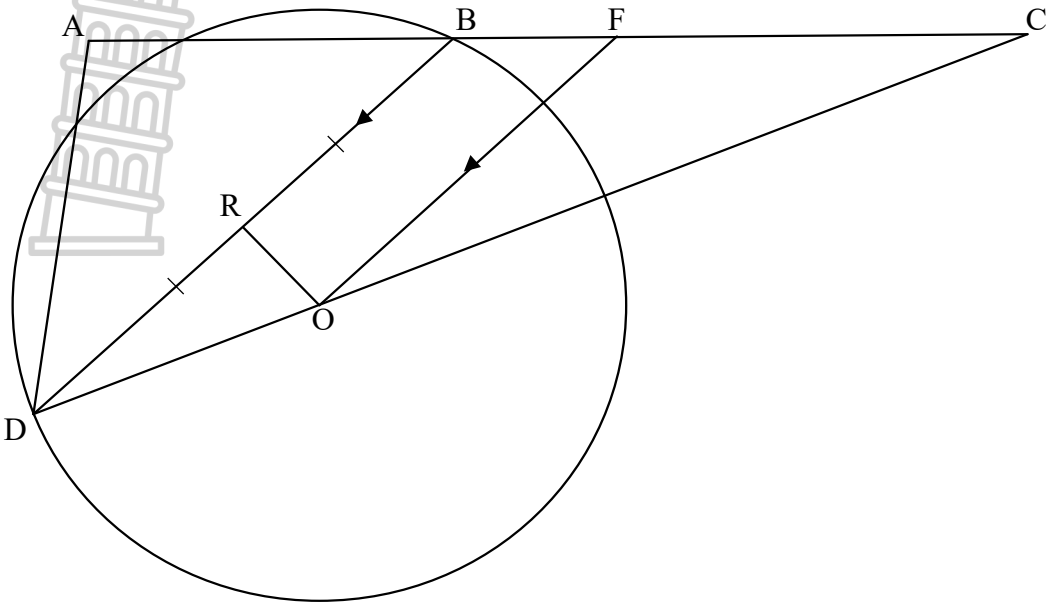
QUESTION/*VRAAG* 10

10.1



10.1	Construction: Draw line MN, where M and N are points on AB and AC respectively such that AM = PK and AN = PL. In Δ AMN and ΔPKL $\hat{A} = \hat{P}$ [given] AM = PK [construction] AN = PL [construction] ΔAMN ≡ ΔPKL [s∠s] $\therefore \hat{M}_1 = \hat{K}$ But $\hat{B} = \hat{K}$ [given] $\therefore \hat{M}_1 = \hat{B}$ ∴ MN ‖ BC [corresp ∠s =/*ooreenk. ∠e* =] $\therefore \frac{AB}{AM} = \frac{AC}{AN}$ [line ‖ one side of Δ/*lyn ‖ een sy v* Δ] But AM = PK and AN = PL $\therefore \frac{AB}{PK} = \frac{AC}{PL}$	✓ construction ✓ S/R ✓ S ✓ S / R ✓ S ✓ R (6)

10.2



10.2.1	In ΔCFO and ΔCBD $\hat{C} = \hat{C}$ [common] $C\hat{F}O = C\hat{B}D$ [corresp ∠s; BD||FO/*ooreenk. ∠e; BD||FO*] $C\hat{O}F = C\hat{D}B$ [sum of ∠s in Δ/*binne ∠e v* Δ] **OR** [corresp ∠s; BD||FO/ *ooreenk. ∠e; BD||FO*] $\Delta CFO \,\|\|\!|\, \Delta CBD$ [∠∠∠]	✓ S ✓ S/R ✓ S/R **OR** R (3)
10.2.2	$\frac{FO}{BD} = \frac{CO}{CD}$ [||| Δs] FO.CD = CO.BD But $R\hat{D}O = F\hat{C}O$ [given] $\therefore$ BD = BC [sides opp equal ∠s/*sye teenoor gelyke ∠e*] $\therefore$ FO.CD = CO.BC	✓ S/R ✓ S/R (2)

10.2.3	RD = 6 units [DR = RB]	
	$\frac{RO}{RD}=\frac{3}{4}$	
	$\therefore RO=\frac{3}{4}(6)$	
	RO = 4,5 units	✓ S
	OR ⊥ BD [line from centre to midpt of chord/ *midpt. sirkel; midpt koord*]	✓ S/R
	$\therefore DO=\sqrt{6^2+4{,}5^2}$ [Pythagoras]	
	DO = 7,5 units	✓ S
	$\frac{BF}{BC}=\frac{DO}{DC}$ [line ‖ to one side of Δ/*lyn* ‖ *een sy v* Δ]	✓ S/R
	OR/*OF* [prop theorem; BD‖FO/*eweredigheidst.;*BD‖FO]	
	BC = BD = 12 units [sides opp equal ∠s/*sye teenoor gelyke ∠e*]	✓ S
	$\therefore \frac{BF}{12}=\frac{7{,}5}{19{,}2}$	✓ S
	$BF=\frac{7{,}5\times 12}{19{,}2}$	
	$BF=\frac{75}{16}$ units	(6)
10.2.4	$\tan R\hat{D}O=\frac{RO}{RD}=\frac{4{,}5}{6}=\frac{3}{4}$	✓ ratio
	$R\hat{D}O = 36{,}87°$	✓ $R\hat{D}O$
	$F\hat{C}O = R\hat{D}O = 36{,}87°$ [given]	
	$\therefore A\hat{B}D = 73{,}74°$ [ext ∠ of Δ/*buite ∠ v.* Δ]	✓ answer (3)
	OR/*OF*	
	$CD^2 = BC^2 + BD^2 - 2(BC)(BD)\cos D\hat{B}C$	
	$\cos D\hat{B}C=\frac{12^2+12^2-19{,}2^2}{2(12)(12)}$	✓ substitution into cosine-rule
	$\cos D\hat{B}C=-\frac{7}{25}$	
	$D\hat{B}C = 106{,}26°$	✓ $D\hat{B}C$
	$\therefore A\hat{B}D = 73{,}74°$ [∠s on a straight line/*∠e op 'n reguitlyn*]	✓ answer (3)
		[20]

TOTAL/*TOTAAL*: 150

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